

MATHEMATISCHES INSTITUT

Vorlesung Differentialgeometrie II Heidelberg, 23.01.2015

Übungsblatt 11

## Some more facts about coverings

To hand in by Friday, January 30, 2015, 12:00

Exercise 1. (20 points)

Let  $p_1: C_1 \longrightarrow B_1$  and  $p_2: C_2 \longrightarrow B_2$  be two coverings. Show that their product  $p_1 \times p_2$  gives a covering of the product space:  $p_1 \times p_2: C_1 \times C_2 \longrightarrow B_1 \times B_2$ .

Exercise 2. (20 points)

Let X be a compact manifold of positive curvature. Show that every map  $f: X \longrightarrow S^1$  is homotopic to a constant map.

*Hints:* Use what you know about the fundamental group of X and the universal covering of  $S^1$ .

Exercise 3. (20 points)

Let X be a topological space. A path-connected subset  $U \subset X$  is called semi-simply connected, if every loop in U is nullhomotopic in X.

Let  $p : C \longrightarrow B$  be a covering, B path-connected und locally path-connected and  $U \subset B$  semi-simply connected. Show that the covering restricted to U is trivial.